Software Quality Metrics Aggregation

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Abstract. Evaluating Software Quality is a critical and very important aspect of software development. There are several metrics developed to assess different characteristics of a software system so as to evaluate its overall quality. One international standard for Software Quality is the ISO/IEC 9126 International Standard; this standard is “proposed to make sure the ‘quality of all software-intensive products’ including safety-critical systems where lives will be at jeopardy if software components fail to succeed.” However, there is no provision to integrate/aggregate different metrics into one value allowing the developer to comprehend rapidly the quality of a software product without having to refer to several different metrics. We propose in this work a way to aggregate different metrics into a single value using a Continuous Logic –the one proposed in Logic Score of Preference (LSP) method.

Keywords: Software Engineering. Continuous Logic. Logic Score of Preferences. LSP Method. Software Quality Metrics. ISO/IEC 9126 Standard.

1 Introduction

In every science and in every engineering branch, quantitative assessment is recognized to be an essential task. Software Engineering is no exception. Software metrics exist practically since the dawn of the area. They are measures of different aspects of software systems, namely size, complexity, quality, etc. The objectives of these metrics are multifold –they are used to assess costs at early stages of systems development, advances along the development, etc.

A number of software metrics have been geared to analyze software quality –e.g. Source Lines Of Code (SLOC)– that have shown to be good metrics to predict defects in software –an important aspect of software quality since good quality is obviously linked to very few if none defects.

The aggregation of different metrics to obtain a single value helps in the global evaluation of a task, project, etc. This need also arises when different metrics are used.

The more traditional aggregation techniques are additive or similar, namely mean, median, or sum. Sometimes these techniques are too crude to be entirely useful. We think that the aggregation methodology should be clear to the analyst, but at the same time sophisticated enough to represent the different aspects of the underlying metrics used and flexible enough so the model can be easily adapted to new quality assurance requirements.

Let us note that there are two sides to software metrics aggregation. One is when applying different metrics –or the same metric– at different levels of granularity of a given piece of software. The other is when applying different metrics –or the same metric– to different software artifacts intended for comparison purposes. In general all aggregation techniques apply to both.
Apart from the simplest strategies of metric aggregation, there are also a number of other methods for aggregation using different techniques, such as those using indexes or coefficients employed in other areas such as econometrics, e.g. Gini [18], Theil [2], coefficients or even the Paretto principle [16].

Other approaches can be found in the literature that propose different methods to aggregate metrics, either using a standard, such as ISO/IEC 9126 or other methodologies. We summarize some of them below.

B. Vasilescu [3] analyzes several aggregation methods for the aggregation of software metrics to measure software quality. This is done from two points of view –first a theoretical analysis is done and then an empirical one is carried out.

In [14] Mordal-Manet et al present not only the problem that metrics alone are not enough to characterize software quality but also an empirical model –the SQuale model [19]– for metric aggregation. This model has four levels adding practices as an intermediate level between criteria and metrics that are the levels suggested in ISO 9126. For assessment purposes SQuale uses an evaluation scale that falls in the interval [0:3], it uses a weighted average, and the function uses a constant to define hard, medium, or soft weighting.

L. Etaati et al in [15] employ a Fuzzy Group Analytical Network Process method to integrate metrics to evaluate e-learning systems. This is a similar method to our proposal however it does not use Continuous Logic functions; moreover the network is not as easy to comprehend as the models obtained from the application of the LSP method.

Bearing the above in mind we have as a main goal to aggregate the data obtained from different quality evaluation metrics in coherent groupings so as to get new singular values that can in turn be aggregated again. The aggregation ends getting a single global indicator for the software object under evaluation, being this object a software unit or an entire software project.

To achieve this process we use operators from a Continuous Logic, specifically the Logic employed by the LSP method that proposes the aggregation of preferences by using a group of logic functions called Generalized Conjunction Disjunction (GCD) operators. So we show here a model –based on the ISO/IEC 9126 international standard [7]– to aggregate software quality metrics employing a Continuous Logic. This standard establishes a number of requirements to evaluate software quality, however there is no prescription for the aggregation of the different measurements proposed. Therefore, there exists the need to propose an aggregation model to obtain a single value out the evaluation with different metrics.

The rest of the article is organized as follows. In Section 2 we give an overview of both the ISO/IEC 9126 standard and of the LSP method. In Section 3 we describe our proposal and illustrate it with some examples. A discussion on the approach, conclusions and future directions for research are given in Section 4.

2 The ISO/IEC 9126 Standard and the LSP Method

To develop our model for software quality evaluation we employ, on the one hand, the ISO/IEC 9126 International Standard for Software Product Quality. On the other hand, to aggregate the metrics proposed in the above mentioned standard, we use a Continuous Logic –the Logic proposed in the Logic Score of Preference (LSP) method. Subsections 2.1 and 2.2 below give an overview of both.
2.1 The ISO/IEC 9126 International Standard

The ISO/IEC 9126 [7] is an international standard that establishes a set of characteristics to evaluate Software Quality. The standard is developed by the International Organization for Standardization (ISO) and the International Electrotechnical Commission (IEC).

Table 1. ISO/IEC 9126 Internal Metrics

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The standard is divided into four parts: quality model, external metrics, internal metrics, and quality in use metrics. The ISO/IEC 9126 quality model sets out six items for the characteristics to be measured. Table 1 shows the six items and their corresponding subitems that correspond to the characteristics that the standard has defined for internal metrics. An internal metric is one that do not rely on software execution (i.e. static measure). It is to be noted that the standard also establishes a list of characteristics for external metrics. External metrics are applicable to running software. Here we have chosen, for illustrating our approach, only internal metrics, although our methodology can be applied to both internal and external metrics.

ISO/IEC 9126 defines these six main characteristics as follows [7]:

**Functionality** metrics are used for predicting if the software product in question will satisfy prescribed functional requirements and implied user needs. It involve the following characteristics:

- **Suitability** that refers to the capability of the software product to provide an appropriate set of functions for specified tasks and user objectives.
- **Accuracy** that refers to the capability of the software product to provide the right or agreed results or effects with the needed degree of precision.
- **Interoperability** that concerns the capability of the software product to interact with one or more specified systems.
- **Security** that refers to the capability of the software product to protect information and data so that unauthorised persons or systems cannot read or modify them and authorised persons or systems are not denied access to them.

- **Functionality Compliance** that addresses the capability of the software product to adhere to standards, conventions or regulations in laws and similar prescriptions relating to functionality.

**Reliability** metrics are used for measuring the capability of software to maintain its level of performance under stated conditions. Reliability is defined by:

- **Maturity** that concern to the capability of the software product to avoid failure as a result of faults in the software.

- **Fault Tolerance** that is the capability of the software product to maintain a specified level of performance in cases of software faults or of infringement of its specified interface.

- **Recoverability** that is the capability of the software product to re-establish a specified level of performance and recover the data directly affected in the case of a failure.

- **Reliability Compliance** that is the capability of the software product to adhere to standards, conventions or regulations relating to reliability.

**Usability** metrics are used for predicting the extent to which the software in question can be understood, learned, operated, attractive and compliant with usability regulations and guidelines. Usability comprises:

- **Understandability** that refers to the capability of the software product to enable the user to understand whether the software is suitable, and how it can be used for particular tasks and conditions of use. It determines the ease of which the systems functions can be understood, relates to user mental models in Human Computer Interaction methods.

- **Learnability** is the capability of the software product to enable the user to learn its application; it relates to the learning effort for different users.

- **Operability** is the capability of the software product to enable the user to operate and control it.

- **Attractiveness** is the capability of the software product to be attractive to the user.

- **Usability Compliance** is the capability of the software product to adhere to standards, conventions, style guides or regulations relating to usability.

**Efficiency** is the capability of the software product to provide appropriate performance, relative to the amount of resources used, under stated conditions. It includes the following characteristics:

- **Time behavior** is the capability of the software product to provide appropriate response and processing times and throughput rates when performing its function, under stated conditions.

- **Resource utilization** is the capability of the software product to use appropriate amounts and types of resources when the software performs its function under stated conditions.

- **Efficiency compliance** is the capability of the software product to adhere to standards or conventions relating to efficiency.

**Maintainability** is the capability of the software product to be modified. Modifications may include corrections, improvements or adaptation of the software to changes in environment, and in requirements and functional specifications.
- **Analyzability**: The capability of the software product to be diagnosed for deficiencies or causes of failures in the software, or for the parts to be modified to be identified.
- **Changeability**: The capability of the software product to enable a specified modification to be implemented.
- **Stability**: The capability of the software product to avoid unexpected effects from modifications of the software.
- **Testability**: The capability of the software product to enable modified software to be validated.
- **Maintainability compliance**: The capability of the software product to adhere to standards or conventions relating to maintainability.

**Portability** is the capability of the software product to be transferred from one environment to another.

- **Adaptability**: The capability of the software product to be adapted for different specified environments without applying actions or means other than those provided for this purpose for the software considered.
- **Installability**: The capability of the software product to be installed in a specified environment.
- **Co-existence**: The capability of the software product to co-exist with other independent software in a common environment sharing common resources.
- **Replaceability**: The capability of the software product to be used in place of another specified software product for the same purpose in the same environment.
- **Portability compliance**: The capability of the software product to adhere to standards or conventions relating to portability.

### 2.2 The Logic Score of Preference Method

The LSP (Logic Score of Preference) method [10], [12], [11], [13], [8], [9] is a method for the creation and use in the evaluation, optimization, comparison, and selection of all kinds of complex systems and not necessarily those based on computers.

Figure 1 shows an overview of the LSP method and its different components.

The method proposes:

(a) The creation of a model of the user’s requirements that is called the **Preference Tree**. On this tree, the **Performance Variables** –that are the main attributes of the system– and their corresponding values are determined. Here the user’s requirements are elicited so as to be incorporated into the Preference Tree.

(b) The definition of functions called **Elementary Criteria**. An Elementary Criterion transforms values from the domain of values a Performance Variable can take into values in the [0,100] interval. These values represent the percentage of compliance of the corresponding requirement and are referred as **Elementary Preferences**.

(c) The creation of an **Aggregation Structure**. The input to this structure are the Elementary Preferences obtained from the application of the defined Elementary Criteria to the Performance Variables. This model is built by aggregating, in as many levels as is deemed necessary, the Elementary Preferences and the intermediate resulting preferences by means of Continuous Logic functions called Generalized Conjunction Disjunction (GCD) operators [13]. The aggregation in intermediate levels gives partial results corresponding to groups of requirements. The complete final model of the Aggregation Structure, also called the LSP criterion function, returns a unique value that is an indicator of the degree of compliance with respect to the total
requirements of the system.

Figure 1. An overview of the LSP evaluation process.

So if we want to aggregate $n$ elementary preferences $E_1, ..., E_n$ in a single preference $E$, the resulting preference $E$—interpreted as the degree of satisfaction of the $n$ requirements—must be expressed as a function having the following properties:

1. The relative importance of each elementary preference $E_i (i = 1,...n)$ can be expressed by a weight $W_i$,  
2. $\min(E_1, ..., E_n) \leq E \leq \max(E_1, ..., E_n)$.

These properties can be achieved using a family of functions (the weighted power means):

$$E(r) = (W_1 E_1^r + W_2 E_2^r + ... + W_n E_n^r)^{1/r}, \text{ where}$$

$$0 < W_i < 100, \ 0 \leq E_i \leq 100, \ i = 1, ..., n, \ W_1 + ... + W_n = 1, \ -\infty \leq r \leq +\infty$$

The choice of $r$ determines the location of $E(r)$ between the minimum value $E_{\min} = \min(E_1, ..., E_n)$ and the maximum value $E_{\max} = \max(E_1, ..., E_n)$, giving place to a Continuous Logic Preference (CPL). For $r = -\infty$ the weighted power mean reduces to the pure conjunction (the minimum function) and for $r = +\infty$ to the pure disjunction (the maximum function). The range between pure conjunction and pure disjunction is usually covered by a sequence of equidistantly located CPL operators (also referred as GCD operators) named: C, C++, C+, C+-, CA, C–+, C–, C--, A, D–, D–+, D+, DA, D++, D.

Once the Aggregation Structure has been calibrated using the different GCD operators and the corresponding weights, then every system under analysis can be evaluated and a single indicator for each can be obtained.
In our case we will obtain—from all the metrics employed—a single aggregated value between 0 and 100 indicating the degree of quality the software under consideration has reached. This value could be contrasted with previous values obtained for the different versions of the same system to assess progress in software quality or against other competing systems under evaluation.

3 The Aggregated Software Evaluation Model

In this section we show a partial aggregation structure illustrating the proposal with some examples.

As we said before the LSP method starts by building a Requirement Tree—a structure that holds all the user’s requirements. In this particular case we start building our Requirement Tree from the ISO/IEC 9126 list of characteristics and sub characteristics as shown in Table 1.

Let us note that the tree shown in Table 1 has only two levels: the first level corresponds to the main software quality characteristics and the second level is where the sub characteristics are. The Requirement Tree will contain at least three levels, being level three where new sub characteristics or particular metrics are. We can find in the literature several different metrics for each sub characteristic in level two, which can be aggregated to obtain a single value.

To illustrate our approach we are going to suppose that a single value has been obtained from the evaluation of each particular metric. In general, these values can be of different data types: real, integer, nominal or categorical (i.e.: bad, poor, fair, good, excellent), etc. They correspond, in the LSP terminology, to the Performance Variables. For each of them, the LSP method proposes the definition of an Elementary Criterion function that takes as its input the value of the corresponding Performance Variable and transforms it to a value in the interval $[0, 100]$; these new values are referred in LSP as Elementary Preferences.

By using the GCD operators we combine these Elementary Preferences to construct an evaluation model or LSP Aggregation Structure. This model corresponds with the user’s needs—in this case the needs to perform a particular software quality evaluation.

Let us suppose that, according to the user’s needs, item 2 (Reliability) has a high significance. This can be represented by penalizing those models whose sub items, namely 2.1, 2.2, 2.3 and 2.4, have values less than a given threshold $u$. Therefore the corresponding Elementary Criteria ($ec_{2,i}$) for items 2.1, 2.2, 2.3 and 2.4, could be defined as in equation (1):

$$ec_{2,i}(x_{2,i}, u_i) = \begin{cases} 
0 & \text{if } x_{2,i} < u_i \\
norm(x_{2,i}) & \text{otherwise}
\end{cases}$$  

(1)

where:

$ec_{2,i}$ is the Elementary Criterion for the Performance Variable $x_{2,i}$ ($1 \leq i \leq 4$).

$\norm$ is a transformation function that returns a value in the interval $[0,100]$.

In Figure 2 we can see an Aggregation Structure where the Elementary Preferences obtained from the application of the Elementary Criteria $ec_{2,i}(x_{2,i}, u_i)$ corresponding to the sub characteristics 2.1 (Maturity), 2.2 (Fault tolerance), 2.3 (Recoverability) and 2.4 (Reliability compliance) have been aggregated using the GCD operator $CA$. $CA$ is a mandatory function meaning that if any of the Elementary Preferences that constitute item 2 is zero (i.e. the value given by the Elementary Criterion defined in equation (1) for each sub characteristic $2.i$) then the mandatory aggregation operator will return zero whichever value the other variables have taken.
Note that apart from being able to choose the GCD function, each of the inputs has an associated weight that plays a part in the final value. In the case shown in Figure 2, item 2.2 has a greater weight than the other items therefore its value will have a bigger impact in the total value of the CA function. This fact has been explained in Section 2.2.

In the example shown in Figure 2 we have chosen the CA function, but in case we wanted to make it more conjunctive making at the same time the aggregated characteristics more mandatory, then the functions C+ or even C could had been chosen.

![Figure 2. The mandatory conjunctive GCD function CA returns 0 if any of the inputs 2.i is 0.](image1)

Sometimes not all the characteristics are essentials (mandatory), some of them could be desirable and others optional, i.e. they can be present or not. This can be achieved using a special aggregation structure, namely Partial Absorption. Figure 3 shows a partial absorption where the attributes 2.1 (Maturity), 2.3 (Recoverability) and 2.4 (Reliability compliance) are considered optional, i.e. they describe characteristics that are strongly wanted but are not absolutely essentials to satisfy the sub tree requirements, while the attribute 2.2 (Fault tolerance) is considered mandatory (essential), i.e. it is an attribute that the system under evaluation must satisfy and whose absence should be penalized so that the whole sub tree is zero.

![Figure 3. Partial Absorption.](image2)

When programmers try to reuse or need to maintain a software system developed by other programmers the difficulty of understanding the system limits reuses. Understandability of software is an important dimension in software usability. In Table 2 we show a part of the Requirement tree corresponding to the sub characteristic 3.1 (Understandability) where we use Halstead Complexity Measures [5] and the cyclomatic number of McCabe [17]. We also include Card and Glass design complexity metrics [4]. Since Card and Glass metrics give a measure of the complexity of the software under analysis they may well be used as a measure of the understandability of the software under evaluation. A design should be as simple as possible. In fact, an elegant design is usually simple. Simplicity facilitates understandability and maintainability.
Table 2. Item 3.1 Understandability.

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<th>3.1.1. Halstead’s complexity.</th>
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<td>3.1.1.1. Calculated length ((n))</td>
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<td>3.1.1.2. Volume ((V))</td>
</tr>
<tr>
<td>3.1.1.3. Difficulty ((D))</td>
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<tr>
<td>3.1.2. McCabe’s cyclomatic number ((M))</td>
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<td>3.1.3. Card &amp; Glass’s complexity</td>
</tr>
<tr>
<td>3.1.3.1. Structural complexity ((S(i)))</td>
</tr>
<tr>
<td>3.1.3.2. Data complexity ((D(i)))</td>
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<tr>
<td>3.1.3.3. System complexity ((C(i)))</td>
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</table>

Halstead has proposed metrics for length and volume of a program based on the number of operators and operands. Halstead’s metrics basically produce—among others—the Program Vocabulary \((n)\), the Program Length \((N)\), the Volume \((V)\) and the Difficulty \((D)\).

The cyclomatic number of McCabe \((M)\) represents the number of linearly independent execution paths through the program. For a well structured module, the cyclomatic number is simply one plus the number of branching statements in the module.

Card and Glass define three measures for design complexity: structural complexity \((S(i))\), data complexity \((D(i))\) and system complexity \((C(i))\). Let us note that the software architectural complexity increases at the same time that the complexity measures increase as well. The complex architecture is inversely proportional to the software understandability.

Figure 4 shows a typical LSP aggregation for the sub structure corresponding to item 3.1 (Understandability). In this aggregation structure the characteristics have been classified in three groups: essential, desirable and optional. Essential parameters are those that describe aspects that the system under evaluation must satisfy and whose absence must be penalized in such a way that the whole sub tree evaluates to zero. Desirable parameters are those that describe features that are strongly desired but are not absolutely essential for satisfying the requirements of the sub tree; therefore its absence does not cause the preference rating to be zero. Optional parameters describe features of a system that are nonessential and whose presence or absence impacts minimally on the overall preference rating of the sub tree.
In this model, we can see that the item 3.1.1 (Halstead Complexity) is more mandatory than the item 3.1.2 (McCabe’s cyclomatic number), which has been considered a desirable requirement. At the same time item 3.1.3 (Card & Glass’s complexity) has been considered optional. These differences are expressed not only through the corresponding weights but also by the assignment of more conjunctive GCD operators as it is shown in the aggregation shown in Figure 4.

Let us note that both the desirable preference (item 3.1.2) and the optional preference (items 3.1.3.x) may be zero, but if the essential preference (item 3.1.1) is not zero, then the aggregate preference will also be not zero. However, in some situations, it may be reasonable to expect that the evaluated systems will have optional and desirable preference that also evaluates to nonzero values. In these cases it is possible to use a simpler aggregation structure as that shown in Figure 5.

In this new aggregation structure we have assumed that desired and optional items are non zero. Under this assumption, the aggregation structure yields similar results as the structure of Figure 4. Obviously, this is a critical assumption since otherwise the zero rating of the desired and optional items would yield a zero rating for the whole structure.

4 Discussion and Future Work

Being able to aggregate all the different metrics in one value is an important asset for software quality analysts since it gives them the ability to compare quickly and simply not only different implementations of the same kind of software –with the same functionality– but it also gives the opportunity to compare different versions of the same software at different development stages.

The aggregation of software quality metrics using the LSP method –presented here– allows a complete aggregation of the desired characteristics but it also allows partial aggregations, namely only one or more metrics of the software quality method chosen and not necessarily the complete ISO/IEC 9126 standard. However, having the complete aggregation model does not limit the capability of having partial results since the LSP model permits the collection of these partial results through partial aggregation structures that are part of the entire model.

Experimenting with different aggregation models is an easy task since, at the very least, it only involves changing functions or weights, especially if a software tool is used to construct and calibrate the model [1].

![Figure 5](image-url)
As part of future work we are considering applying the proposed approach in a more industrial setting comparing different versions of a given software as well as a same kind of software product developed by different software development teams. We also believe that the approach presented here can be further explored extending it to other standards such as ISO/IEC 14598 [6] that is sometimes used in conjunction with ISO/IEC 9126 amongst others.

References


